

# Hadronic centrality dependence in nuclear collisions

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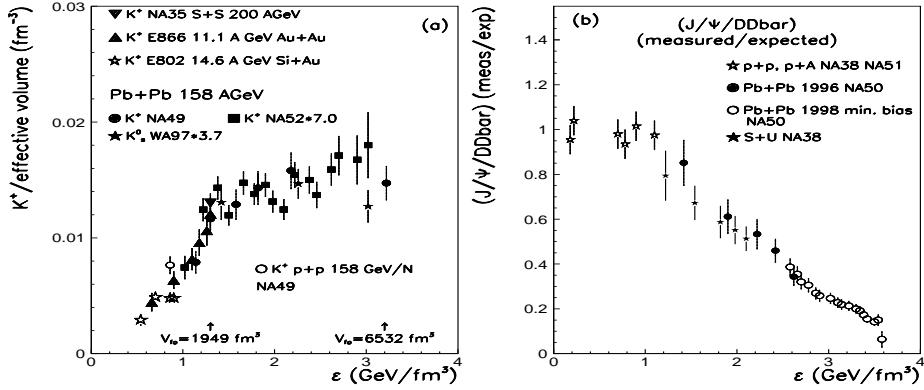
**Abstract.** The kaon number density in nucleus+nucleus and p+p reactions is investigated for the first time as a function of the initial energy density  $\epsilon$  and is found to exhibit a discontinuity around  $\epsilon=1.3$  GeV/fm<sup>3</sup>. This suggests a higher degree of chemical equilibrium for  $\epsilon > 1.3$  GeV/fm<sup>3</sup>. It can also be interpreted as reflection of the same discontinuity, appearing in the chemical freeze out temperature (T) as a function of  $\epsilon$ . The  $N^{\alpha \sim 1}$  dependence of (u,d,s) hadrons, with N the number of participating nucleons, also indicates a high degree of chemical equilibrium and T saturation, reached at  $\epsilon > 1.3$  GeV/fm<sup>3</sup>. Assuming that the intermediate mass region (IMR) dimuon enhancement seen by NA50 is due to open charm ( $D\bar{D}$ ), the following observation can be made: a) Charm is not equilibrated. b)  $J/\Psi/D\bar{D}$  suppression -unlike  $J/\Psi/DY$ - appears also in S+A collisions, above  $\epsilon \sim 1$  GeV/fm<sup>3</sup>. c) Both charm and strangeness show a discontinuity near the same  $\epsilon$ . d)  $J/\Psi$  could be formed mainly through  $c\bar{c}$  coalescence. e) The enhancement factors of hadrons with u,d,s,c quarks may be connected in a simple way to the mass gain of these particles if they are produced out of a quark gluon plasma (QGP). We discuss these results as possible evidence for the QCD phase transition occurring near  $\epsilon \sim 1.3$  GeV/fm<sup>3</sup>.

## 1. Introduction

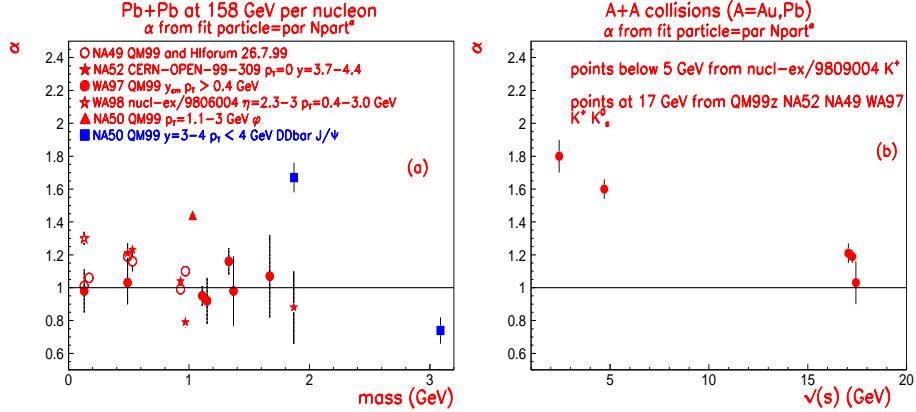
The quark-gluon plasma phase transition predicted by QCD [1] may occur and manifest itself in ultrarelativistic nuclear collisions through discontinuities in the initial energy density ( $\epsilon_i$ ) dependence of relevant observables. A major example of a discontinuity is seen in the  $J/\Psi/DY$  [2] discussed e.g. in [3, 4]. We investigate here for the first time the dependence of strangeness production, in particular of kaons, on the initial energy density  $\epsilon_i$ . The degree of equilibrium achieved in nuclear collisions has been intensively studied comparing hadron ratios and densities to models (see e.g. [4, 5, 6, 7]). We investigate here if chemical equilibrium is achieved, examining another aspect of equilibrium states, namely the volume ( $V$ ) independence of hadron densities ( $\rho$ ).

## 2. Results and discussion

The kaon density ( $\rho_K$ =(K per collision)/V) at the thermal freeze out in nuclear reactions, investigated as a function of the initial energy density  $\epsilon_i$  (figure 1,(a)) (see [8] for calculation details), exhibits a dramatic changeover around  $\epsilon=1.3$  GeV/fm<sup>3</sup>, saturating for higher  $\epsilon$  values, while it is falling below. The syst. error on  $\epsilon_i$  is estimated to be  $\sim 30\%$ . It is assumed that the number of nucleons participating in the collision (N) is proportional to the volume of the particle source at the thermal freeze out [8]. The new results from Si+Au at 14.6 A GeV and p+p at 158 A GeV shown in figure 1, which are not included in [8], have been estimated using data from [9] and methods described in [8]. Furthermore,  $\rho_K$  rises with N respectively with V below  $\epsilon=1.3$  GeV/fm<sup>3</sup> while it does not depend on N respectively on V above  $\epsilon=1.3$  GeV/fm<sup>3</sup>. To illustrate this, two values of V are noted on figure 1. The changes of  $K^\pm$  and  $\pi^\pm$  with N within the Pb+Pb system, have been first realized in [10]. A



**Figure 1.** Initial energy density ( $\epsilon$ ) dependence of: (a) The  $K^+$  multiplicity over the effective volume of the particle source at thermal freeze out. (b) The  $J/\Psi/DDbar$  (measured/'expected') ratio [8].



**Figure 2.** The parameter  $\alpha$ , resulting from the  $N^\alpha$  fit to hadron yields shown as a function of (a): the mass of the particles in the region  $\epsilon > 1.3 \text{ GeV/fm}^3$  at SPS and (b) of the  $\sqrt{s}$ , for kaons.  $N$  is the number of participating nucleons.

similar behaviour as the one seen in figure 1, can be inferred for pions as well as for the  $K/\pi$  ratio (S.K. work in progress). The  $N^\alpha$  exponent of hadrons with (u,d,s) quarks above  $\epsilon = 1.3 \text{ GeV/fm}^3$ , do not depend on the particle mass (figure 2, (a)). At  $\epsilon > 1.3 \text{ GeV/fm}^3$   $\alpha$  is near to one, as expected in case of a chemically equilibrated state, assuming  $N \sim V$ . The deviations seen in  $\phi$ ,  $\pi^0$  and  $\bar{p}$  may be due to the transverse momentum acceptance. Therefore, figure 2 (a) supports the assumption of a high degree of chemical equilibrium reached above  $\epsilon = 1.3 \text{ GeV/fm}^3$ , among hadrons with u,d,s quarks. The  $N^\alpha$  exponent of kaons is found to depend strongly on  $\sqrt{s}$  for kaons (figure 2,(b)). Therefore, below  $\epsilon = 1.3 \text{ GeV/fm}^3$ ,  $\rho_K$  (figure 1 and figure 2 (b)),  $\rho_\pi$  and the  $K/\pi$  ratio, show an increase with increasing  $N$  respectively with  $V$ .

Figures 1 and 2 can be interpreted in two ways. Firstly, kaons may achieve a higher degree of chemical equilibrium only for  $\epsilon > 1.3 \text{ GeV/fm}^3$ , and may not be fully

equilibrated below [8]. The equilibration of strangeness is expected in a QGP and its observation at  $\epsilon \sim 1.3 \text{ GeV/fm}^3$  could therefore be a sign of a transition to QGP. In this case, it is a transition from a non equilibrated hadron gas to an equilibrated QGP. It is therefore not a well defined phase transition in the thermodynamic sense. Secondly, kaons can be in fact chemically equilibrated also below  $\epsilon = 1.3 \text{ GeV/fm}^3$ , and the change respectively the constancy of  $\rho_K$  with  $V_{fo}$  and  $\epsilon_i$  observed in figure 1, can be a result of the increase of the freeze out temperature with  $\epsilon_i$  below  $\epsilon = 1.3 \text{ GeV/fm}^3$ , respectively of the stability of  $T_{fo}$  above  $1.3 \text{ GeV/fm}^3$ . This dependence of  $T_{fo}$  on  $\epsilon_i$ , namely rising until it reaches a critical  $T_c$  value and saturating above for all reactions, would strongly support the QCD phase transition appearing at  $\epsilon \sim 1.3 \text{ GeV/fm}^3$ . This interpretation fully agrees with thermal models which suggest that particle ratios at freeze out are compatible with thermalization even in A+A collisions at 1 A GeV [5]. However the first interpretation is not in gross disagreement with [5], because there the thermal model description is modified (introducing e.g.  $\rho_k \sim V$ ) in order to describe the data at 1 A GeV.

Furthermore, the correct interpretation can be corroborated by further investigations discussed in the following. The nonzero baryochemical potential ( $\mu_B$ ), which in the reactions shown in figure 1, happens to change with  $\epsilon_i$ , makes the interpretation of figure 1 difficult. Therefore, it appears that the dependence of the temperature at chemical freeze out extrapolated to  $\mu_b=0$ , on  $\epsilon_i$ , would help to identify and prove the QCD phase transition. A rising and then a for ever saturating freeze out temperature above  $\epsilon = 1.3 \text{ GeV/fm}^3$  is a strong argument that the QCD phase transition occurs at this  $\epsilon$ , and figure 1 is a direct consequence of it.

The question if the QCD phase transition appears at the critical  $\epsilon_i$  in any volume, or if there is additionally a critical initial volume of the particle source above which the transition takes place, can be answered comparing QGP signatures in systems with different volumes but the same  $\epsilon_i$ . For example comparing  $p + p$ ,  $e^+e^-$  etc collisions to heavy ion collisions e.g. at the same  $\epsilon$ . This is not yet done for the signature of the  $J/\Psi$  suppression and it has to be clarified e.g. using Tevatron data [8]. For the signature of strangeness enhancement it is suggested by figure 1 in [6] that there is indeed a critical initial volume, only above which strangeness is enhanced over  $p + \bar{p}$  at the same  $\epsilon_i$ . This conclusion follows, if we assume that Tevatron reaches at least  $\epsilon_i$  values similar to SPS A+A collisions [11] and if figure 1 in [6] is not biased by the model calculation [6].

If strangeness is indeed not equilibrated at  $\epsilon < 1.3 \text{ GeV/fm}^3$ , this may explain the decrease of the double ratio  $(K/\pi)(A+A/p+p)$  with increasing  $\sqrt{s}$ . In particular, a larger strangeness annihilation is enforced by equilibrium at SPS reducing the strange particle yield. However the assumption of non equilibrium of  $s\bar{s}$  at low  $\epsilon$  is not necessary here, since the above observation can be possibly traced back to e.g. the variation of  $\mu_B(A + A)/\mu_B(p + p)$  with  $\sqrt{s}$  in A+A collisions. Furthermore, in the context of QGP formation, it seems irrelevant to discuss e.g.  $s\bar{s}$  enhancement in A+B over p+p collisions in a nonequilibrium situation. It is the very establishment of equilibrium in the (u,d,s) sector, which can reveal informations on QGP.

The kaon number densities in p+p and A+B collisions in figure 1, (a) are similar, when compared at the same  $\epsilon_i$ . See also [12] for a discussion of universality of pion phase space densities.

Our prediction for the N dependence of hadrons at RHIC and LHC is the  $N^1$  thermal limit, as long as hadron yields are dominated by low transverse momentum particles. Furthermore, if the changeover of  $\rho_k$  at  $\epsilon = 1.3 \text{ GeV/fm}^3$  shown in figure 1 is due to

the QCD phase transition, we predict for RHIC and LHC the same total strangeness (or kaon) number density and the same freeze out temperature, -after correction for the  $\mu_B$  dependence-, as for  $\epsilon = 1.3\text{--}3.0 \text{ GeV/fm}^3$ . If this change is however due to the onset of equilibrium in a hadronic gas, and the QCD phase transition takes place at higher  $\epsilon$ , it may manifest itself through a second changeover of hadron number densities, ratios and freeze out temperatures -after correction for the different  $\mu_B$ - e.g. in RHIC above  $\epsilon \sim 3 \text{ GeV/fm}^3$ .

Assuming that the IMR dimuon enhancement seen by NA50 is due to open charm, the following observations can be made: a) open charm appears not to be equilibrated ( $\alpha = 1.7$ ) (figure 2, (a)) [8]. b) The  $J/\Psi/D\bar{D}$  ratio deviates from p+p and p+A data also in S+U collisions (figure 1, (b)), above  $\epsilon \sim 1 \text{ GeV/fm}^3$ . c) It therefore appears that both charm and strangeness show a discontinuity near the same  $\epsilon \sim 1 \text{ GeV/fm}^3$  [8], similar to the critical  $\epsilon_c \sim 1\text{--}2 \text{ GeV/fm}^3$  predicted by QCD [1, 3]. d) The N dependence of the  $J/\Psi/D\bar{D}$  ratio can be interpreted as the  $J/\Psi$  being formed through  $c, \bar{c}$  coalescence [8]. e) Finally, the enhancement factors of hadrons with u,d,s,c quarks may be connected in a simple way to the mass gain of these particles in the quark gluon plasma (table below) [13].  $T_q$  are the enhancement factors of the lightest mesons with u,d,s,c quarks ( $\pi, K, D$ ), if they are produced out of a quark gluon plasma (e.g.  $g + g \rightarrow s + \bar{s}$  (1)), as compared to their direct production from hadron interactions away from the transition point (e.g.  $p + p \rightarrow K^+ + \Lambda + p$  (2)). The gain is taken proportional to  $m_{\text{particle}} - m_{\text{quarks}}$ , as this expresses the different thresholds of reactions (1) and (2). In the table below the predicted enhancement factors ( $T_q$ ) of hadrons with u,d,s,c quarks from a QGP are compared to the experimentally measured ones ( $E_q$ ), and are found to be similar. (Definitions:  $th_q = m_0 - m_q$ ,  $m_{u,d} = 7 \text{ MeV}$ ,  $m_s = 175 \text{ MeV}$ ,  $m_c = 1.25 \text{ GeV}$ ,  $m_0 = m(\pi, K, D)$ ).

Quark flavour	$th_q$	$T_q = \sqrt{th_q/th_{u,d}}$	$E_{(N+N)}^{(A+B)}$	$E_q = E/E_{u,d}$
u,d	133	1	$\pi/N \sim 1.12$	1
s	320	1.55	$K/N \sim 2$	1.79
c	615	2.15	$D\bar{D}$ meas/exp $\sim 3$	2.68

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